

6. [In this question, the unit vectors \mathbf{i} and \mathbf{j} are in a vertical plane, \mathbf{i} being horizontal and \mathbf{j} being vertically upwards.]

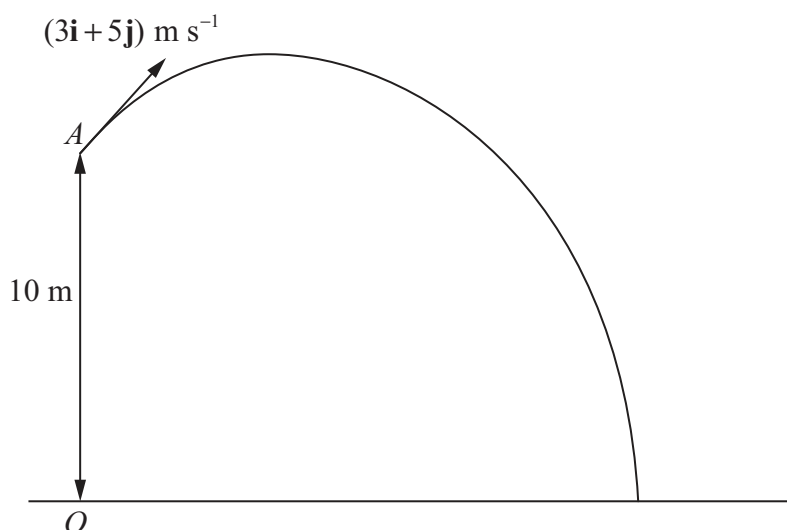


Figure 3

At time $t = 0$, a particle P is projected from the point A which has position vector $10\mathbf{j}$ metres with respect to a fixed origin O at ground level. The ground is horizontal. The velocity of projection of P is $(3\mathbf{i} + 5\mathbf{j}) \text{ m s}^{-1}$, as shown in Figure 3. The particle moves freely under gravity and reaches the ground after T seconds.

- (a) For $0 \leq t \leq T$, show that, with respect to O , the position vector, \mathbf{r} metres, of P at time t seconds is given by

$$\mathbf{r} = 3t\mathbf{i} + (10 + 5t - 4.9t^2)\mathbf{j} \tag{3}$$

- (b) Find the value of T . (3)

- (c) Find the velocity of P at time t seconds ($0 \leq t \leq T$). (2)

When P is at the point B , the direction of motion of P is 45° below the horizontal.

- (d) Find the time taken for P to move from A to B . (2)

- (e) Find the speed of P as it passes through B . (2)



